

Let g be some deterministic function from $\{0, 1\}^k$ to $\{0, 1\}$ and \mathcal{A} be a randomized algorithm that on input $x \in \{0, 1\}^k$ outputs $y \in \{0, 1\}$. It holds that $\mathcal{A}(x) = g(x)$ with probability p , and $\mathcal{A}(x) = 1 - g(x)$ otherwise. Note that k is in \mathbb{N} .

1. Assuming $p = 3/4$, describe an estimator algorithm \mathcal{E} that estimates $g(x)$ for a specific input x using \mathcal{A} as a subroutine and fails with probability less than e^{-k} . Describe your estimator, analyze its probability of success and also its running time.
2. Assuming $p = 1/2 + f(k)$, how small can $f(k)$ be so that an estimator invoking \mathcal{A} at most polynomial number of times in k fails with probability less than e^{-k} ?